# Statistical Machine Learning: Dynamical, Stochastic and Economic Perspectives 

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## Musings on Computation in Statistics

- Two main perspectives: Optimization and Sampling


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- Two main perspectives: Optimization and Sampling
- underlying mathematical objects: derivatives and integrals
- Are they just incommensurate? Frequentist vs Bayesian?
- Surely not---mature disciplines blend the two
- cf. vector-field and Lagrangian/Hamiltonian perspectives in mechanics


## Musings (Cont)

- In the current era, work on optimization and sampling is quite different
- the latter focuses on equilibrium states
- the former focuses on trajectories


## Musings (Cont)

- In the current era, work on optimization and sampling is quite different
- the latter focuses on equilibrium states
- the former focuses on trajectories
- Glimmers of relationships
- hybrid Monte Carlo
- geometric connections (Riemannian and symplectic)
- analyses of SDEs that include dimension dependence
- variational inference


## Statistics and Computation

- A Grand Challenge of our era: tradeoffs between statistical inference and computation
- most data analysis problems have a time budget
- and they're often embedded in a control problem
- Optimization has provided the computational model for this effort (computer science, not so much)
- it's provided the algorithms and the insights


## Statistics and Computation (cont)

- Modern large-scale statistics has posed new challenges for optimization
- millions of variables, millions of terms, sampling issues, nonconvexity, need for confidence intervals, paralleldistributed platforms, etc


## Statistics and Computation (cont)

- Modern large-scale statistics has posed new challenges for optimization
- millions of variables, millions of terms, sampling issues, nonconvexity, need for confidence intervals, paralleldistributed platforms, etc
- Current focus: what can we do with the following ingredients?
- gradients
- stochastics
- acceleration


## Algorithmic and Theoretical Progress

- Nonconvex optimization
- avoidance of saddle points
- rates that have dimension dependence
- acceleration, dynamical systems and lower bounds
- statistical guarantees from optimization guarantees
- Computationally-efficient sampling
- nonconvex functions
- nonreversible MCMC
- links to optimization
- Market design
- approach to saddle points
- recommendations and two-way markets


## Sampling vs. Optimization: The Tortoise and the Hare

- Folk knowledge: Sampling is slow, while optimization is fast
- but sampling provides inferences, while optimization only provides point estimates
- But there hasn't been a clear theoretical analysis that establishes this folk knowledge as true
- Is it really true?



## Sampling vs. Optimization: The Tortoise and the Hare

- I'll present a class of problems for which a discretized Langevin diffusion has a polynomial convergence rate in terms of dimension
- Whereas any gradient-based optimization procedure necessarily has an exponential convergence rate


# Part I: How to Escape Saddle Points Efficiently 

with Chi Jin, Praneeth Netrapalli, Rong Ge, and Sham Kakade



## Nonconvex Optimization in Machine Learning

- Bad local minima used to be thought of as the main problem on the optimization side of machine learning
- But many machine learning architectures either have no local minima (see list later), or stochastic gradient seems to have no trouble (eventually) finding global optima
- But saddle points abound in these architectures, and they cause the learning curve to flatten out, perhaps (nearly) indefinitely


## The Importance of Saddle Points



Strict saddle point


Non-strict saddle point

- How to escape?
- need to have a negative eigenvalue that's strictly negative
- How to escape efficiently?
- in high dimensions how do we find the direction of escape?
- should we expect exponential complexity in dimension?


## A Few Facts

- Gradient descent will asymptotically avoid saddle points (Lee, Simchowitz, Jordan \& Recht, 2017)
- Gradient descent can take exponential time to escape saddle points (Du, Jin, Lee, Jordan, \& Singh, 2017)
- Stochastic gradient descent can escape saddle points in polynomial time (Ge, Huang, Jin \& Yuan, 2015)
- but that's still not an explanation for its practical success
- Can we prove a stronger theorem?


## Optimization

Consider problem:

$$
\min _{\mathbf{x} \in \mathbb{R}^{d}} f(\mathbf{x})
$$

Gradient Descent (GD):

$$
\mathbf{x}_{t+1}=\mathbf{x}_{t}-\eta \nabla f\left(\mathbf{x}_{t}\right) .
$$

Convex: converges to global minimum; dimension-free iterations.


## Convergence to FOSP

Function $f(\cdot)$ is $\ell$-smooth (or gradient Lipschitz)

$$
\forall \mathbf{x}_{1}, \mathbf{x}_{2},\left\|\nabla f\left(\mathbf{x}_{1}\right)-\nabla f\left(\mathbf{x}_{2}\right)\right\| \leq \ell\left\|\mathbf{x}_{1}-\mathbf{x}_{2}\right\| .
$$

Point $\mathbf{x}$ is an $\epsilon$-first-order stationary point ( $\epsilon$-FOSP) if

$$
\|\nabla f(\mathbf{x})\| \leq \epsilon
$$

## Theorem [GD Converges to FOSP (Nesterov, 1998)]

For $\ell$-smooth function, GD with $\eta=1 / \ell$ finds $\epsilon$-FOSP in iterations:

$$
\frac{2 \ell\left(f\left(x_{0}\right)-f^{\star}\right)}{\epsilon^{2}}
$$

*Number of iterations is dimension free.

## Nonconvex Optimization

Non-convex: converges to Stationary Point (SP) $\nabla f(\mathbf{x})=0$.
SP : local min / local max / saddle points


Many applications: no spurious local min (see full list later).

## Definitions and Algorithm

Function $f(\cdot)$ is $\rho$-Hessian Lipschitz if

$$
\forall \mathbf{x}_{1}, \mathbf{x}_{2},\left\|\nabla^{2} f\left(\mathbf{x}_{1}\right)-\nabla^{2} f\left(\mathbf{x}_{2}\right)\right\| \leq \rho\left\|\mathbf{x}_{1}-\mathbf{x}_{2}\right\|
$$

Point $\mathbf{x}$ is an $\epsilon$-second-order stationary point $(\epsilon$-SOSP) if

$$
\|\nabla f(\mathbf{x})\| \leq \epsilon, \quad \text { and } \quad \lambda_{\min }\left(\nabla^{2} f(\mathbf{x})\right) \geq-\sqrt{\rho \epsilon}
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## Algorithm Perturbed Gradient Descent (PGD)

1. for $t=0,1, \ldots$ do
2. if perturbation condition holds then
3. $\quad \mathbf{x}_{t} \leftarrow \mathbf{x}_{t}+\xi_{t}, \quad \xi_{t}$ uniformly $\sim \mathbb{B}_{0}(r)$
4. $\quad \mathbf{x}_{t+1} \leftarrow \mathbf{x}_{t}-\eta \nabla f\left(\mathbf{x}_{t}\right)$

Adds perturbation when $\left\|\nabla f\left(\mathbf{x}_{t}\right)\right\| \leq \epsilon$; no more than once per $T$ steps.

## Main Result

## Theorem [PGD Converges to SOSP]

For $\ell$-smooth and $\rho$-Hessian Lipschitz function $f$, PGD with $\eta=O(1 / \ell)$ and proper choice of $r, T$ w.h.p. finds $\epsilon$-SOSP in iterations:

$$
\tilde{O}\left(\frac{\ell\left(f\left(\mathbf{x}_{0}\right)-f^{\star}\right)}{\epsilon^{2}}\right)
$$

*Dimension dependence in iteration is $\log ^{4}(d)$ (almost dimension free).

|  | GD(Nesterov 1998) | PGD(This Work) |
| :---: | :---: | :---: |
| Assumptions | $\ell$-grad-Lip | $\ell$-grad-Lip $+\rho$-Hessian-Lip |
| Guarantees | $\epsilon$-FOSP | $\epsilon$-SOSP |
| Iterations | $2 \ell\left(f\left(\mathbf{x}_{0}\right)-f^{\star}\right) / \epsilon^{2}$ | $\tilde{O}\left(\ell\left(f\left(\mathbf{x}_{0}\right)-f^{\star}\right) / \epsilon^{2}\right)$ |

## Geometry and Dynamics around Saddle Points

Challenge: non-constant Hessian + large step size $\eta=O(1 / \ell)$.
Around saddle point, stuck region forms a non-flat "pancake" shape.


Key Observation: although we don't know its shape, we know it's thin! (Based on an analysis of two nearly coupled sequences)

## How Fast Can We Go?

- Important role of lower bounds (Nemirovski \& Yudin)
- strip away inessential aspects of the problem to reveal fundamentals
- The acceleration phenomenon (Nesterov)
- achieve the lower bounds
- second-order dynamics
- a conceptual mystery
- Our perspective: it's essential to go to continuous time
- the notion of "acceleration" requires a continuum topology to support it


# Part II: Variational, Hamiltonian and Symplectic Perspectives on Acceleration 

with Andre Wibisono, Ashia Wilson and Michael Betancourt



## Accelerated gradient descent

Setting: Unconstrained convex optimization

$$
\min _{x \in \mathbb{R}^{d}} f(x)
$$

- Classical gradient descent:

$$
x_{k+1}=x_{k}-\beta \nabla f\left(x_{k}\right)
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obtains a convergence rate of $O(1 / k)$

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x_{k+1}=x_{k}-\beta \nabla f\left(x_{k}\right)
$$

obtains a convergence rate of $O(1 / k)$

- Accelerated gradient descent:

$$
\begin{aligned}
& y_{k+1}=x_{k}-\beta \nabla f\left(x_{k}\right) \\
& x_{k+1}=\left(1-\lambda_{k}\right) y_{k+1}+\lambda_{k} y_{k}
\end{aligned}
$$

obtains the (optimal) convergence rate of $O\left(1 / k^{2}\right)$

## Accelerated methods: Continuous time perspective

- Gradient descent is discretization of gradient flow

$$
\dot{X}_{t}=-\nabla f\left(X_{t}\right)
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(and mirror descent is discretization of natural gradient flow)

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- Su, Boyd, Candes '14: Continuous time limit of accelerated gradient descent is a second-order ODE

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- These ODEs are obtained by taking continuous time limits. Is there a deeper generative mechanism?

Our work: A general variational approach to acceleration
A systematic discretization methodology

## Bregman Lagrangian

$$
\mathcal{L}(x, \dot{x}, t)=e^{\gamma_{t}+\alpha_{t}}\left(D_{h}\left(x+e^{-\alpha_{t}} \dot{x}, x\right)-e^{\beta_{t}} f(x)\right)
$$

Variational problem over curves:

$$
\min _{X} \int \mathcal{L}\left(X_{t}, \dot{X}_{t}, t\right) d t
$$



Optimal curve is characterized by Euler-Lagrange equation:

$$
\frac{d}{d t}\left\{\frac{\partial \mathcal{L}}{\partial \dot{x}}\left(X_{t}, \dot{X}_{t}, t\right)\right\}=\frac{\partial \mathcal{L}}{\partial x}\left(X_{t}, \dot{X}_{t}, t\right)
$$

E-L equation for Bregman Lagrangian under ideal scaling:

$$
\ddot{X}_{t}+\left(e^{\alpha_{t}}-\dot{\alpha}_{t}\right) \dot{X}_{t}+e^{2 \alpha_{t}+\beta_{t}}\left[\nabla^{2} h\left(X_{t}+e^{-\alpha_{t}} \dot{X}_{t}\right)\right]^{-1} \nabla f\left(X_{t}\right)=0
$$

## Mysteries

- Why can't we discretize the dynamics when we are using exponentially fast clocks?
- What happens when we arrive at a clock speed that we can discretize?
- How do we discretize once it's possible?


## Towards A Symplectic Perspective

- We've discussed discretization of Lagrangian-based dynamics
- Discretization of Lagrangian dynamics is often fragile and requires small step sizes
- We can build more robust solutions by taking a Legendre transform and considering a Hamiltonian formalism:

$$
\begin{aligned}
L(q, v, t) & \rightarrow H(q, p, t, \mathcal{E}) \\
\left(\frac{\mathrm{d} q}{\mathrm{~d} t}, \frac{\mathrm{~d} v}{\mathrm{~d} t}\right) & \rightarrow\left(\frac{\mathrm{d} q}{\mathrm{~d} \tau}, \frac{\mathrm{~d} p}{\mathrm{~d} \tau}, \frac{\mathrm{~d} t}{\mathrm{~d} \tau}, \frac{\mathrm{~d} \mathcal{E}}{\mathrm{~d} \tau}\right)
\end{aligned}
$$

## Symplectic Integration of Bregman Hamiltonian



## Symplectic vs Nesterov



## Symplectic vs Nesterov



# Part III: Acceleration and Saddle Points 

with Chi Jin and Praneeth Netrapalli

## Hamiltonian Analysis



## Convergence Result

## PAGD Converges to SOSP Faster (Jin et al. 2017)

For $\ell$-gradient Lipschitz and $\rho$-Hessian Lipschitz function $f$, PAGD with proper choice of $\eta, \theta, r, T, \gamma, s$ w.h.p. finds $\epsilon$-SOSP in iterations:

$$
\tilde{O}\left(\frac{\ell^{1 / 2} \rho^{1 / 4}\left(f\left(x_{0}\right)-f^{\star}\right)}{\epsilon^{7 / 4}}\right)
$$

|  | Strongly Convex | Nonconvex (SOSP) |
| :---: | :---: | :---: |
| Assumptions | $\ell$-grad-Lip \& |  |
| (Perturbed) GD | $\alpha$-str-convex | $\rho$-Hessian-Lip |
| (Perturbed) AGD | $\tilde{O}(\ell / \alpha)$ | $\tilde{O}\left(\Delta_{f} \cdot \ell / \epsilon^{2}\right)$ |
| Condition $\kappa$ | $\tilde{O}(\sqrt{\ell / \alpha})$ | $\tilde{O}\left(\Delta_{f} \cdot \ell^{\frac{1}{2}} \rho^{\frac{1}{4}} / \epsilon^{\frac{7}{4}}\right)$ |
| Improvement | $\ell / \alpha$ | $\ell / \sqrt{\rho \epsilon}$ |

# Part IV: Acceleration and Stochastics 

## with Xiang Cheng, Niladri Chatterji and Peter Bartlett

## Acceleration and Stochastics

- Can we accelerate diffusions?
- There have been negative results...
- ...but they've focused on classical overdamped diffusions


## Acceleration and Stochastics

- Can we accelerate diffusions?
- There have been negative results...
- ...but they've focused on classical overdamped diffusions
- Inspired by our work on acceleration, can we accelerate underdamped diffusions?


## Overdamped Langevin MCMC

Described by the Stochastic Differential Equation (SDE):

$$
d x_{t}=-\nabla U\left(x_{t}\right) d t+\sqrt{2} d B_{t}
$$

where $U(x): R^{d} \rightarrow R$ and $B_{t}$ is standard Brownian motion.
The stationary distribution is $p^{*}(x) \propto \exp (U(x))$

Corresponding Markov Chain Monte Carlo Algorithm (MCMC):

$$
\tilde{x}_{(k+1) \delta}=\tilde{x}_{k \delta}-\nabla U\left(\tilde{x}_{k \delta}\right)+\sqrt{2 \delta} \xi_{k}
$$

where $\delta$ is the step-size and $\xi_{k} \sim N\left(0, I_{d \times d}\right)$

## Guarantees under Convexity

Assuming $U(x)$ is $L$-smooth and $m$-strongly convex:
Dalalyan'14: Guarantees in Total Variation
If $n \geq O\left(\frac{d}{\epsilon^{2}}\right)$ then, $T V\left(p^{(n)}, p^{*}\right) \leq \epsilon$
Durmus \& Moulines'16: Guarantees in 2-Wasserstein

$$
\text { If } n \geq O\left(\frac{d}{\epsilon^{2}}\right) \text { then, } W_{2}\left(p^{(n)}, p^{*}\right) \leq \epsilon
$$

Cheng and Bartlett'17: Guarantees in KL divergence

$$
\text { If } n \geq O\left(\frac{d}{\epsilon^{2}}\right) \text { then, } \operatorname{KL}\left(p^{(n)}, p^{*}\right) \leq \epsilon
$$

## Underdamped Langevin Diffusion

Described by the second-order equation:

$$
\begin{aligned}
& d x_{t}=v_{t} d t \\
& d v_{t}=-\gamma v_{t} d t+\lambda \nabla U\left(x_{t}\right) d t+\sqrt{2 \gamma \lambda} d B_{t}
\end{aligned}
$$

The stationary distribution is $p^{*}(x, v) \propto \exp \left(-U(x)-\frac{|v|_{2}^{2}}{2 \lambda}\right)$
Intuitively, $x_{t}$ is the position and $v_{t}$ is the velocity
$\nabla U\left(x_{t}\right)$ is the force and $\gamma$ is the drag coefficient

## Quadratic Improvement

Let $p^{(n)}$ denote the distribution of $\left(\tilde{x}_{n \delta}, \tilde{v}_{n \delta}\right)$. Assume $U(x)$ is strongly convex

Cheng, Chatterji, Bartlett, Jordan '17:
If $n \geq O\left(\frac{\sqrt{d}}{\epsilon}\right)$ then $W_{2}\left(p^{(n)}, p^{*}\right) \leq \epsilon$

Compare with Durmus \& Moulines '16 (Overdamped)
If $n \geq O\left(\frac{d}{\epsilon^{2}}\right)$ then $W_{2}\left(p^{(n)}, p^{*}\right) \leq \epsilon$

## Proof Idea: Reflection Coupling

Tricky to prove continuous-time process contracts. Consider two processes,

$$
\begin{aligned}
& d x_{t}=-\nabla U\left(x_{t}\right) d t+\sqrt{2} d B_{t}^{x} \\
& d y_{t}=-\nabla U\left(y_{t}\right) d t+\sqrt{2} d B_{t}^{y}
\end{aligned}
$$

where $x_{0} \sim p_{0}$ and $y_{0} \sim p^{*}$. Couple these through Brownian motion

$$
d B_{t}^{y}=\left[I_{d \times d}-\frac{2 \cdot\left(x_{t}-y_{t}\right)\left(x_{t}-y_{t}\right)^{\top}}{\left|x_{t}-y_{t}\right|_{2}^{2}}\right] d B_{t}^{x}
$$

"reflection along line separating the two processes"

## Reduction to One Dimension

By Itô's Lemma we can monitor the evolution of the separation distance

$$
d\left|x_{t}-y_{t}\right|_{2}=-\left\langle\frac{x_{t}-y_{t}}{\left|x_{t}-y_{t}\right|_{2}}, \nabla U\left(x_{t}\right)-\nabla U\left(y_{t}\right)\right\rangle d t+2 \sqrt{2} d B_{t}^{1}
$$

'1-d random walk'
Two cases are possible

1. If $\left|x_{t}-y_{t}\right|_{2} \leq R$ then we have strong convexity; the drift helps.
2. If $\left|x_{t}-y_{t}\right|_{2} \geq R$ then the drift hurts us, but Brownian motion helps stick" Rates not exponential in $d$ as we have a 1-d random walk

## Part VI: Acceleration and Sampling

With Yi-An Ma, Niladri Chatterji, and Xiang Cheng

## Acceleration of SDEs

- The underdamped Langevin stochastic differential equation is Nesterov acceleration on the manifold of probability distributions, with respect to the KL divergence (Ma, et al., to appear)


# Part V: Population Risk and Empirical Risk 

with Chi Jin and Lydia Liu


## Population Risk vs Empirical Risk



Well-behaved population risk

$\Rightarrow \quad$ rough empirical risk

- Even when $R$ is smooth, $\hat{R}_{n}$ can be non-smooth and may even have many additional local minima (ReLU deep networks).
- Typically $\left\|R-\hat{R}_{n}\right\|_{\infty} \leq O(1 / \sqrt{n})$ by empirical process results.

Can we finds local min of $R$ given only access to the function value $\hat{R}_{n}$ ?

## Our Contribution

Our answer: Yes! Our SGD approach finds $\epsilon-$ SOSP of $F$ if $\nu \leq \epsilon^{1.5} / d$, which is optimal among all polynomial queries algorithms.


Complete characterization of error $\nu$ vs accuracy $\epsilon$ and dimension $d$.

## Part VII: Market Design Meets GradientBased Learning

with Lydia Liu, Horia Mania and Eric Mazumdar


## Two Examples of Current Projects

- How to find saddle points in high dimensions?
- not just any saddle points; we want to find the Nash equilibria (and only the Nash equilibria)
- Competitive bandits and two-way markets
- how to find the "best action" when supervised training data is not available, when other agents are also searching for best actions, and when there is conflict (e.g., scarcity)




## Perspectives on AI

- The classical "human-imitative" perspective
- cf. Al in the movies, interactive home robotics
- The "intelligence augmentation" (IA) perspective
- cf. search engines, recommendation systems, natural language translation
- the system need not be intelligent itself, but it reveals patterns that humans can make use of
- The "intelligent infrastructure" (II) perspective
- cf. transportation, intelligent dwellings, urban planning
- large-scale, distributed collections of data flows and looselycoupled decisions
M. Jordan (2018), "Artificial Intelligence: The Revolution Hasn't Happened Yet", Medium.


## What Intelligent Systems Currently Exist?

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- Brains and Minds



## What Intelligent Systems Currently Exist?

- Brains and Minds

- Markets




## AI = Data + Algorithms + Markets

- Computers are currently gathering huge amounts of data, for and about humans, to be fed into learning algorithms
- often the goal is to learn to imitate humans
- a related goal is to provide personalized services to humans
- but there's a lot of guessing going on about what people want
- Services are best provided in the context of a market; market design can eliminate much of the guesswork
- when data flows in a market, the underlying system can learn from that data, so that the market provides better services
- fairness arises not from providing the same service to everyone, but by allowing individual utilities to be expressed
- Learning algorithms provide the glue between data and the market


## Consider Classical Recommendation Systems

- A record is kept of each customer's purchases
- Customers are "similar" if they buy similar sets of items
- Items are "similar" are they are bought together by multiple customers


## Consider Classical Recommendation <br> Systems

- A record is kept of each customer's purchases
- Customers are "similar" if they buy similar sets of items
- Items are "similar" are they are bought together by multiple customers
- Recommendations are made on the basis of these similarities
- These systems have become a commodity


## Multiple Decisions with Competition

- Suppose that recommending a certain movie is a good business decision (e.g., because it's very popular)
- Is it OK to recommend the same movie to everyone?
- Is it OK to recommend the same book to everyone?
- Is it OK to recommend the same restaurant to everyone?
- Is it OK to recommend the same street to every driver?
- Is it OK to recommend the same stock purchase to everyone?


## The Alternative: Create a Market

- A two-way market between consumers and producers
- based on recommendation systems on both sides
- E.g., diners are one side of the market, and restaurants on the other side
- E.g., drivers are one side of the market, and street segments on the other side
- This isn't just classical microeconomics; the use of recommendation systems is key


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## Social Consequences

- By creating a market based on the data flows, new jobs are created!
- So here's a way that AI can be a job creator, and not (mostly) a job killer
- This can be done in a wide range of other domains, not just music
- entertainment
- information services
- personal services
- The markets-meets-learning approach deals with other problems that a pure learning approach does not
- e.g., recommendations when there is scarcity


## Example: Music in the Data Age

- More people are making music than ever before, placing it on sites such as SoundCloud
- More people are listening to music than ever before
- But there is no economic value being exchanged between producers and consumers
- And, not surprisingly, most people who make music cannot do it as their full-time job
- i.e., human happiness is being left on the table


## Example: Music in the Data Age

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- But there is no economic value being exchanged between producers and consumers
- And, not surprisingly, most people who make music cannot do it as their full-time job
- i.e., human happiness is being left on the table
- There do exist companies who make money off of this; they stream data from SoundCloud to listeners, and they make their money ... from advertising! :


## The Alternative: Create a Market

- Use data to provide a dashboard to musicians, letting them learn where their audience is
- The musician can give shows where they have an audience
- And they can make offers to their fans


## The Alternative: Create a Market

- Use data to provide a dashboard to musicians, letting them learn where their audience is
- The musician can give shows where they have an audience
- And they can make offers to their fans
- I.e., consumers and producers become linked, and value flows: a market is created
- the company that creates this market profits simply by taking a cut from the transactions


## Executive Summary

- ML (AI) has come of age
- But it is far from being a solid engineering discipline that can yield robust, scalable solutions to modern dataanalytic problems
- There are many hard problems involving uncertainty, inference, decision-making, robustness and scale that are far from being solved
- not to mention economic, social and legal issues

